

Worksheet 9

Let (G, \cdot) be a group.

1. Prove that the identity of G is unique.
2. Prove that inverses in G are unique.
3. Define a binary operation $*$ on \mathbb{Z} by $a * b = a + b - 1$. Show that $(\mathbb{Z}, *)$ forms a group.